# Introduction to normalization <br> Lecture 06.01 

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## Relational Schema Design

- Goal of relational schema design is to avoid anomalies and redundancy.
- Update anomaly : one occurrence of a fact is changed, but not all occurrences.
- Deletion anomaly: valid fact is lost when a tuple is deleted.
- Now we will tackle the problem of refining relational schemas.
- The main method: decomposition of relations into smaller relations


## Normalization

- Database normalization is the process of organizing the fields and tables of a relational database to minimize redundancy and dependency
- Normalization involves dividing large tables into smaller (and less redundant) tables and defining relationships between them.
- The objective: isolate each fact so that additions, deletions, and modifications of a field can be made in just one table and then propagated through the rest of the database using the defined relationships


## The goals of normalization defined by Codd:

1. To free the collection of relations from undesirable insertion, update and deletion dependencies
2. To reduce the need for restructuring the collection of relations, as new types of data are introduced, and thus increase the life span of application programs
3. To make the relational model more informative to users
4. To make the collection of relations neutral to the query statistics, where these statistics are liable to change as time goes by

- E.F. Codd,
"Further Normalization of the Data Base Relational Model"


## Functional dependencies

- The primary key identifies an entity
- All non-key attributes are functionally dependent on the key
- It is a special type of a function - a database function: knowing an argument (value of attribute(s) A), we can find all the other attributes (not from a formula but by lookup)
- Notation: $A \rightarrow B$
- $A$ uniquely identifies $B$
- $B$ is functionally dependent on $A$


## Example of functional dependencies

| Grades |  |  |
| :--- | :--- | :--- |
| Name | Course | Grade |
| Bob | Databases | In pr |
| Maria | HCl | A |
| John | Python | B |
| Tom | HCl | A |
| Maria | Algorithms | A |
| Bob | HCl | B |
| Maria | Python | A |

Name, Course $\rightarrow$ Grade Name $\rightarrow$ Grade<br>Grade $\rightarrow$ Course<br>Course $\rightarrow$ Grade

- Functional dependencies reflect real-life facts and are nothing else but constraints on data


## FD example

- Constraint: "no two courses can meet in the same room at the same time"
\{hour, room $\} \rightarrow$ course


## Example: database of student records

Students (Name, Courses (with grades))

## Students

| Name | Courses |
| :--- | :--- |
| Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| John | Python (B) |
| Tom | $\mathrm{HCl}(\mathrm{A})$ |
| Maria | Algorithms (A), Python(A), $\mathrm{HCl}(\mathrm{A})$ |

Constraints:
Name is unique
One student may take multiple courses

Usage:
Report one student's courses and grades

## The first thing- identify key

- The key of the relation is a set of one or more attributes that identify each tuple (row)
- The value of a key is unique for each row
- Each relation has only one key
- Key is immutable: once the value of the key is assigned to a tuple, it cannot be updated through the lifetime of the database, but only deleted with the entire tuple
- All non-key attributes are functionally dependent on key


## Database of student records: key?

Students (Name, Courses (with grades))

## Students

| Name | Courses |
| :--- | :--- |
| Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| John | Python (B) |
| Tom | $\mathrm{HCl}(\mathrm{A})$ |
| Maria | Algorithms (A), Python(A), HCl(A) |

## Student records: key defined

Students (ID, Name, Courses (with grades))

| Students |  |  |
| :--- | :--- | :--- |
| ID | Name | Courses |
| $\mathbf{1}$ | Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{2}$ | John | Python (B) |
| $\mathbf{3}$ | Tom | HCl (A) |
| $\mathbf{4}$ | Maria | Algorithms (A), Python(A), HCl(A) |

Updated constraints:
ID is unique
ID determines Name
ID determines courses

## Student records: functional dependencies

Students (ID, Name, Courses (with grades))

| Students |  |  |
| :--- | :--- | :--- |
| ID | Name | Courses |
| $\mathbf{1}$ | Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{2}$ | John | Python (B) |
| $\mathbf{3}$ | Tom | $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{4}$ | Maria | Algorithms (A), Python(A), HCl(A) |

ID $\rightarrow$ Name
ID $\rightarrow$ Courses
ID, Name $\rightarrow$ Courses

# Student record database is anomalous 

Students (ID, Name, Courses (with grades))

## Students

| ID | Name | Courses |
| :--- | :--- | :--- |
| $\mathbf{1}$ | Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{2}$ | John | Python (B) |
| $\mathbf{3}$ | Tom | $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{4}$ | Maria | Algorithms (A), Python(A), $\mathrm{HCl}(\mathrm{A})$ |

- There is no redundancy (good!)
- Insertion anomaly
- Deletion anomaly
- General-purpose queries are inefficient


## Normal forms -testing for normalization

- The database is normalized when all its relations are normalized
- There are rules to test each relation - normal forms:
- 1NF
- 2NF
- 3NF
- BCNF
- 4NF
- 5NF
- In most cases, the relation is normalized if it is in 3NF


## First normal form 1NF

- The primary key is defined
- The domain of each attribute is represented as a single column (no duplicative attributes with the same meaning)
- Every row-and-column intersection contains exactly one value from the applicable domain (atomicity)


## Students: in 1NF?

| Students relation |  |  |
| :--- | :--- | :--- |
| ID | Name | Courses |
| $\mathbf{1}$ | Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{2}$ | John | Python (B) |
| $\mathbf{3}$ | Tom | HCl (A) |
| $\mathbf{4}$ | Maria | Algorithms (A), Python(A), $\mathrm{HCl}(\mathrm{A})$ |

## Students: in 1NF?

| Students relation |  |  |
| :--- | :--- | :--- |
| ID | Name | Courses |
| $\mathbf{1}$ | Bob | Databases (in progr.), $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{2}$ | John | Python (B) |
| $\mathbf{3}$ | Tom | $\mathrm{HCl}(\mathrm{A})$ |
| $\mathbf{4}$ | Maria | Algorithms (A), Python(A), $\mathrm{HCl}(\mathrm{A})$ |

- The courses are not atomic: each cell in this column contains multiple values


## Students: in 1NF?

Students relation

| ID | Name | Course1 | Grade1 | Course2 | Grade2 | Course3 | Grade3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Bob | Databases | In progr. | HCl | A |  |  |
| $\mathbf{2}$ | John | Python | B |  |  |  |  |
| $\mathbf{3}$ | Tom | HCl | A |  |  |  |  |
| $\mathbf{4}$ | Maria | Algorithms | A | Phyton | A | HCl | A |

## Students: in 1NF?

| Students relation |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| ID | Name | Course1 | Grade1 | Course2 | Grade2 | Course3 | Grade3 |
| $\mathbf{1}$ | Bob | Databases | In progr. | HCl | A |  |  |
| $\mathbf{2}$ | John | Python | B |  |  |  |  |
| $\mathbf{3}$ | Tom | HCl | A |  |  |  |  |
| $\mathbf{4}$ | Maria | Algorithms | A | Phyton | A | HCl | A |

- The attributes are duplicative (multiple columns for the same domain)
- Still general queries are difficult
- Waste of space
- Limited number of courses per student


## Students: in 1NF?

Students (ID, Name, Course, Grade)

| Students |  |  |  |
| :--- | :--- | :--- | :--- |
| ID | Name | Course | Grade |
| $\mathbf{1}$ | Bob | Databases | In pr |
| $\mathbf{2}$ | Maria | HCl | A |
| $\mathbf{3}$ | John | Python | B |
| $\mathbf{4}$ | Tom | HCl | A |
| $\mathbf{2}$ | Maria | Algorithms | A |
| $\mathbf{1}$ | Bob | HCl | B |
| $\mathbf{2}$ | Maria | Python | A |

## Primary key?

## Students: in 1NF!

Students (ID, Name, Course, Grade)

Students

| ID | Course | Name | Grade |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Databases | Bob | In pr |
| $\mathbf{2}$ | HCl | Maria | A |
| $\mathbf{3}$ | Python | John | B |
| $\mathbf{4}$ | HCl | Tom | A |
| $\mathbf{2}$ | Algorithms | Maria | A |
| $\mathbf{1}$ | HCl | Bob | B |
| $\mathbf{2}$ | Python | Maria | A |

## New data: Students extended

Students (ID, Course, Name, Phone, Major, Professor, Grade)

Students

| ID | Course | Name | Phone | Major |  | Prof |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Grade |  |  |  |  |  |  |
| $\mathbf{1}$ | Databases | Bob | $211-2112$ | CSCl | Dr. Monk | In pr |
| $\mathbf{2}$ | HCI | Maria | $344-3344$ | BIOL | Dr. Pooh | A |
| $\mathbf{3}$ | Python | John | $500-5005$ | MATH | Dr. Patel | B |
| $\mathbf{4}$ | HCI | Tom | $601-6778$ | PHYS | Dr. Pooh | A |
| $\mathbf{2}$ | Algorithms | Maria | $344-3344$ | BIOL | Dr. Monk | A |
| $\mathbf{1}$ | HCI | Bob | $211-2112$ | CSCl | Dr. Pooh | B |
| $\mathbf{2}$ | Python | Maria | $344-3344$ | BIOL | Dr. Patel | A |

## Students extended

Students (ID, Course, Name, Phone, Major, Professor, Grade)

Students

| ID | Course | Name | Phone | Major | Prof | Grade |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Databases | Bob | $211-2112$ | CSCl | Dr. Monk | In pr |
| $\mathbf{2}$ | HCl | Maria | $344-3344$ | BIOL | Dr. Pooh | A |
| $\mathbf{3}$ | Python | John | $500-5005$ | MATH | Dr. Patel | B |
| $\mathbf{4}$ | $\underline{\text { HCl }}$ | Tom | $601-6778$ | PHYS | Dr. Pooh | A |
| $\mathbf{2}$ | $\underline{\text { Algorithms }}$ | Maria | $344-3344$ | BIOL | Dr. Monk | A |
| $\mathbf{1}$ | $\underline{\text { HCl }}$ | Bob | $211-2112$ | CSCl | Dr. Pooh | B |
| $\mathbf{2}$ | $\underline{\text { Python }}$ | Maria | $344-3344$ | BIOL | Dr. Patel | A |

Constraints:

- ID is unique
- Student can take many courses
- Student majors in one subject
- Student has only one phone
- Course is taught by one professor


## Students extended

Students (ID, Course, Name, Phone, Major, Professor, Grade)

Students

| ID | Course | Name | Phone | Major | Prof | Grade |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Databases | Bob | $211-2112$ | CSCl | Dr. Monk | In pr |
| $\mathbf{2}$ | HCl | Maria | $344-3344$ | BIOL | Dr. Pooh | A |
| $\mathbf{3}$ | Python | John | $500-5005$ | MATH | Dr. Patel | B |
| $\mathbf{4}$ | $\underline{\text { HCl }}$ | Tom | $601-6778$ | PHYS | Dr. Pooh | A |
| $\mathbf{2}$ | $\underline{\text { Algorithms }}$ | Maria | $344-3344$ | BIOL | Dr. Monk | A |
| $\mathbf{1}$ | $\underline{\text { HCl }}$ | Bob | $211-2112$ | CSCl | Dr. Pooh | B |
| $\mathbf{2}$ | Python | Maria | $344-3344$ | BIOL | Dr. Patel | A |

Constraints (functional dependencies)

- ID $\rightarrow$ Name
- ID $\rightarrow$ Phone
- ID $\rightarrow$ Major
- Course $\rightarrow$ Professor
- ID, Course $\rightarrow$ Grade


## Students extended: problems

Students (ID, Course, Name, Phone, Major, Professor, Grade)

## Students

| ID | Course | Name | Phone | Major | Prof | Grade |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Databases | Bob | $211-2112$ | CSCl | Dr. Monk | In pr |
| $\mathbf{2}$ | HCI | Maria | $344-3344$ | BIOL | Dr. Pooh | A |
| $\mathbf{3}$ | Python | John | $500-5005$ | MATH | Dr. Patel | B |
| $\mathbf{4}$ | HCI | Tom | $601-6778$ | PHYS | Dr. Pooh | A |
| $\mathbf{2}$ | Algorithms | Maria | $344-3344$ | BIOL | Dr. Monk | A |
| $\mathbf{1}$ | HCI | Bob | $211-2112$ | CSCl | Dr. Pooh | B |
| $\mathbf{2}$ | Python | Maria | $344-3344$ | BIOL | Dr. Patel | A |

- Redundancy
- Insertion anomaly
- Deletion anomaly
- Update anomaly


## Second normal form: 2NF

- The relation is in 1NF
- All non-key attributes are fully dependent on the key (no attributes depend on a part of a key)


## Functional dependency diagram



## Extended Students: in 2NF?



Partial dependencies

## Extended Students: in 2NF?



- Solution: decompose all partial dependencies into separate relations

Partial dependencies

## Students in 2NF

| Students |  |  |  |
| :--- | :--- | :--- | :--- |
| ID | Name | Phone | Major |
| $\mathbf{1}$ | Bob | $211-2112$ | CSCI |
| $\mathbf{2}$ | Maria | $344-3344$ | BIOL |
| $\mathbf{3}$ | John | $500-5005$ | MATH |
| $\mathbf{4}$ | Tom | $601-6778$ | PHYS |


| Grades |  |  |
| :--- | :--- | :--- |
| ID | Course | Grade |
| 1 | Databases | In pr |
| 2 | HCl | A |
| 3 | Python | B |
| 4 | HCl | A |
| 2 | Algorithms | A |
| 1 | HCl | B |
| 2 | Python | A |



Students (ID, Name, Phone, Major)
Courses (Course, Prof)
Grades (ID, Course, Grade)

## Students relation: new information

## Students (ID, Name, Phone, Major, Department)

| Students |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{I D}$ | Name | Phone | Major | Department |
| $\mathbf{1}$ | Bob | $211-2112$ | CSCI | Computer Science |
| $\mathbf{2}$ | Maria | $344-3344$ | BIOL | Life Sciences |
| $\mathbf{3}$ | John | $500-5005$ | MATH | Mathematics and Statistics |
| $\mathbf{4}$ | Tom | $601-6778$ | PHYS | Physics |
| $\mathbf{5}$ | Andrew | $222-2341$ | CSCI | Computer Science |
| $\mathbf{6}$ | Ann | $544-6778$ | STAT | Mathematics and Statistics |

New constraint:
Major $\rightarrow$ Department

## Students relation: new information

Students (ID, Name, Phone, Major, Department)

| Students |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| ID | Name | Phone | Major | Department |
| $\mathbf{1}$ | Bob | $211-2112$ | CSCl | Computer Science |
| $\mathbf{2}$ | Maria | $344-3344$ | BIOL | Life Sciences |
| $\mathbf{3}$ | John | $500-5005$ | MATH | Mathematics and Statistics |
| $\mathbf{4}$ | Tom | $601-6778$ | PHYS | Physics |
| $\mathbf{5}$ | Andrew | $222-2341$ | CSCI | Computer Science |
| $\mathbf{6}$ | Ann | $544-6778$ | STAT | Mathematics and Statistics |

- Redundancy
- Update anomalies

Major $\rightarrow$ Department

## Third normal form 3NF

- The relation is in 2NF
- All attributes are functionally dependent only on the key: no dependency on another non-key attribute


## Functional dependency diagram



## Functional dependency diagram



Transitive dependency

## Students in 3NF

Students

| ID | Name | Phone | Major |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Bob | $211-2112$ | CSCI |
| $\mathbf{2}$ | Maria | $344-3344$ | BIOL |
| $\mathbf{3}$ | John | $500-5005$ | MATH |
| $\mathbf{4}$ | Tom | $601-6778$ | PHYS |
| $\mathbf{5}$ | Andrew | $222-2341$ | CSCI |
| $\mathbf{6}$ | Ann | $544-6778$ | STAT |

Students (ID, Name, Phone, Major)
MajorsOffered (Major, Department)

| MajorsOffered |  |
| :--- | :--- |
| Major | Department |
| CSCI | Computer Science |
| BIOL | Life Sciences |
| PHYS | Physics |
| MATH | Mathematics and Statistics |
| STAT | Mathematics and Statistics |



## Boyce-Codd normal form - BCNF

- Relation is in 3NF
- All attributes depend on the key, full key and nothing but the key


## Professor workload: in BCNF?

|  | Professors |  |  |
| :--- | :--- | :--- | :--- |
| Prof | Department | Head | WorkLoad |
| Dr. Monk | CSCI | Prof. Ming | $30 \%$ |
| Dr. Pooh | MATH | Prof. Doe | $70 \%$ |
| Dr. Patel | PHYS | Prof. Bond | $100 \%$ |
| Dr. Pooh | CSCI | Prof. Ming | $30 \%$ |
| Dr. Monk | BIOL | Prof. Bond | $30 \%$ |
| Dr. Monk | MATH | Prof. Doe | $40 \%$ |

Department $\rightarrow$ Head
Prof, Department $\rightarrow$ Workload

## Functional dependency diagram



Two overlapping
composite
candidate keys

## Functional dependency diagram



- BCNF violation: part of two candidate keys depends on another part

Two overlapping
composite
candidate keys

## Professors in BCNF

| Professors |  |  |
| :--- | :--- | :--- |
| Prof | Department | WorkLoad |
| Dr. Monk | CSCI | $30 \%$ |
| Dr. Pooh | MATH | $70 \%$ |
| Dr. Patel | PHYS | $100 \%$ |
| Dr. Pooh | CSCI | $30 \%$ |
| Dr. Monk | BIOL | $30 \%$ |
| Dr. Monk | MATH | $40 \%$ |


| Department |  |
| :--- | :--- |
| Department | Head |
| CSCI | Prof. Ming |
| MATH | Prof. Doe |
| PHYS | Prof. Bond |
| BIOL | Prof. Bond |
|  |  |

Professors (Prof, Department, Workload) Department (Department, Head)

Apply

| Order ID |  | Customer | Phone | Item1 | Qty1 | Price1 | Item2 | Qty2 | Price2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | Bob | $211-2112$ | Pen | 2 | 5.49 | Eraser | 1 | 2.00 |  |
| $\mathbf{2}$ | John | $344-3344$ | Pen | 5 | 5.49 |  |  |  |  |
| $\mathbf{3}$ | Bob | $211-2112$ | Pen | 1 | 5.49 |  |  |  |  |
| $\mathbf{4}$ | Maria | $500-5005$ | Eraser | 3 | 2.00 |  |  |  |  |

## Relationship between normal forms



